

STScI NGST Libration Point Introduction

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History, Definitions, & Modeling



History

Euler

- Defined three body problem in work on lunar motion.
- Proved existence of co-linear points

Lagrange

- Development of equilibrium points

Poincare

- Stability of motion and use of potential functions
- First to recognize the need for a qualitative approach to three body problem which is unsolvable in closed form

Jacobi

- One exact integral of three body system

Definitions & Modeling

- Easiest to model the system as the Circular Restricted Three Body Problem (CRTBP) where $m_1 \gg m_2 \gg m_3$
 - ↳ m_1 - primary, m_2 - secondary, m_3 - body of interest
 - ↳ motion of Earth about Sun is circular
 - ↳ motion of m_3 is in plane of m_1 & m_2
- CRTBP can be solved exactly
- Unfortunately, unmodeled forces (solar radiation pressure, other gravitational bodies - Jupiter, etc.) and physical reality (non-circular motion or EM system about sun) cause perturbations



The Libration Points

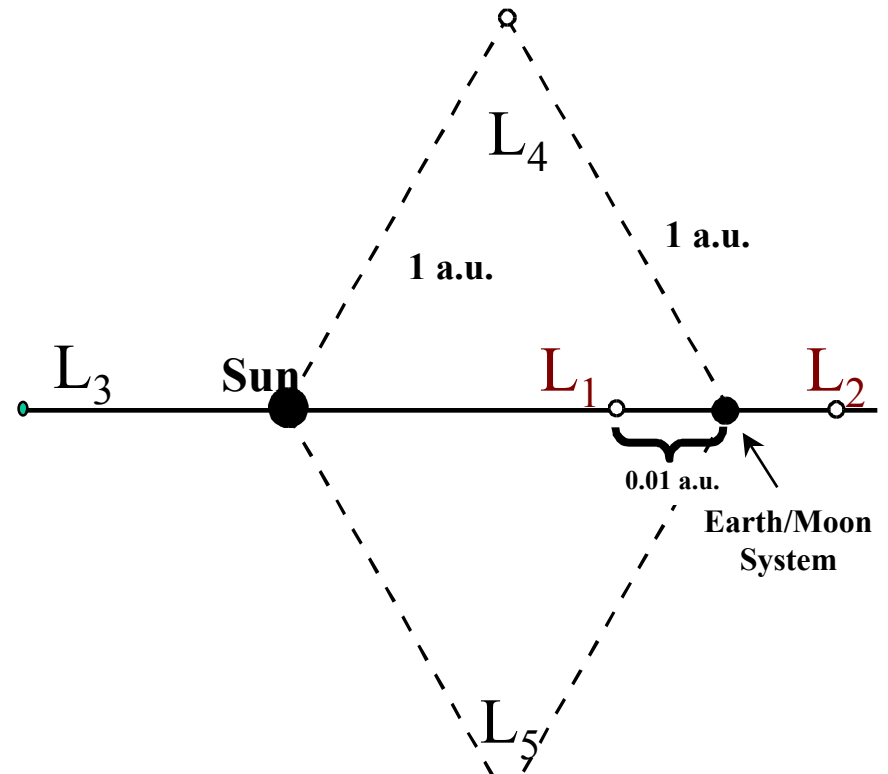


What Are They??

- Equilibrium or libration points represent singularities in the equations of motion where velocity and acceleration components are zero and the forces are balanced
- Viewed in the rotating frame: centrifugal (Coriolis-Type) force balances with gravitational forces of the two primaries
- Libration points are in plane with no Z component
- Our system of interest involves the Sun (m_1), the Earth-Moon system (m_2) and the spacecraft m_3

Where Are They?

- Collinear Points: L_1 , L_2 , L_3 (unstable)
- Triangular Points: L_4 , L_5 (stable)

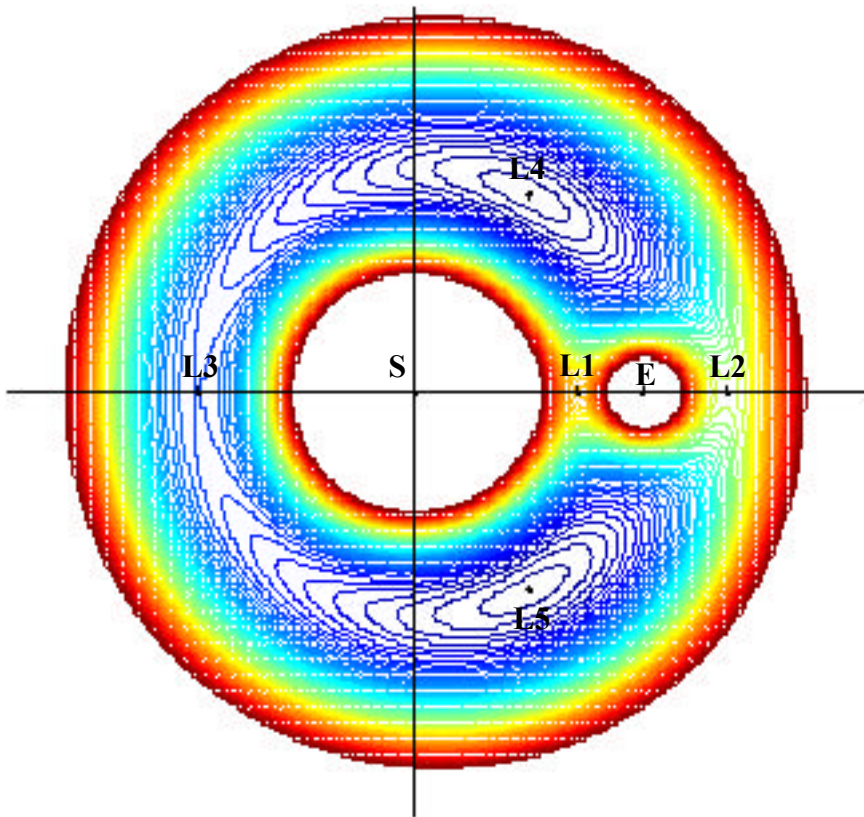


Solar Rotating Coordinates
Ecliptic Plane Projection

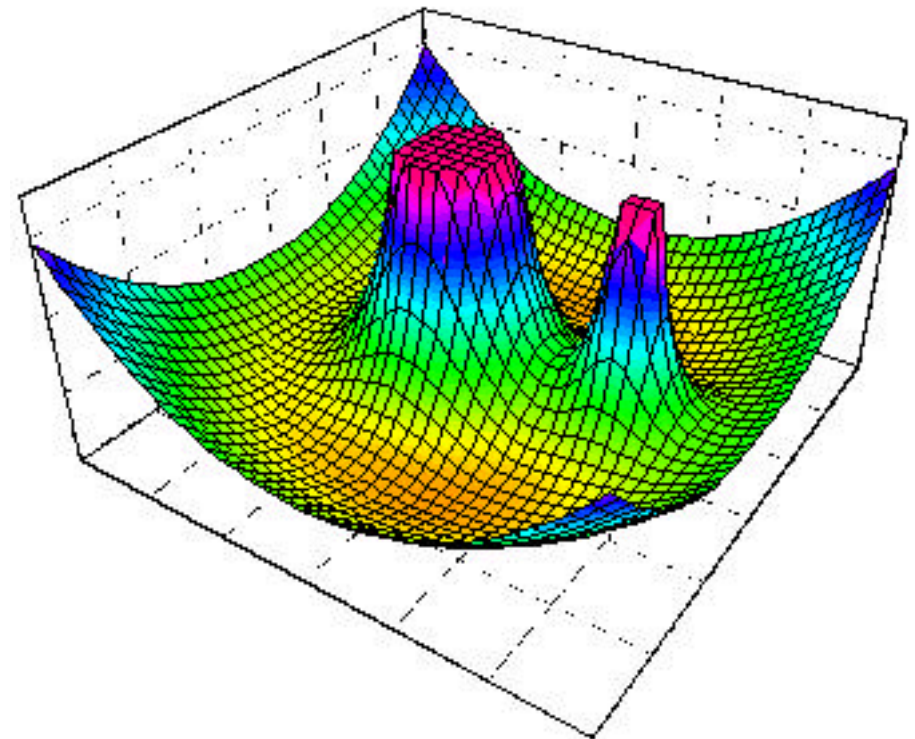
Potential for Planar CRTBP

$$V^2 = x^2 + y^2 + [2(1-\mu)/r_1] + [2\mu/r_2] - C$$

2-D View (Ecliptic Projection)



3-D View of Potential (fixed C)





Motion About the Libration Points



- Periodic solutions can be found for motion about the collinear libration points in the CRTBP

- ↪ $x = K A_Y \sin (x_{XY} t + x_{XY})$

- ↪ $y = A_Y \cos (x_{XY} t + x_{XY})$

- ↪ $z = A_Z \sin (z t + z)$

- Period of motion about libration points is 180 days

- There are two types of motion about libration points

- ↪ Lissajous orbits

- ☞ $x_{XY} = z$

- ☞ As a result, the orbit oscillates about the y-axis such that the projection along the sun-line seems to open and close

- ☞ Because of this motion, constraints on a solar exclusion zone or eclipse region may be required

- ↪ Halo orbits

- ☞ Special solution of the libration point orbit where $x_{XY} = z$ and $A_Y > 655,000$ km



Lissajous Patterns (MAP)



14 Year Evolution

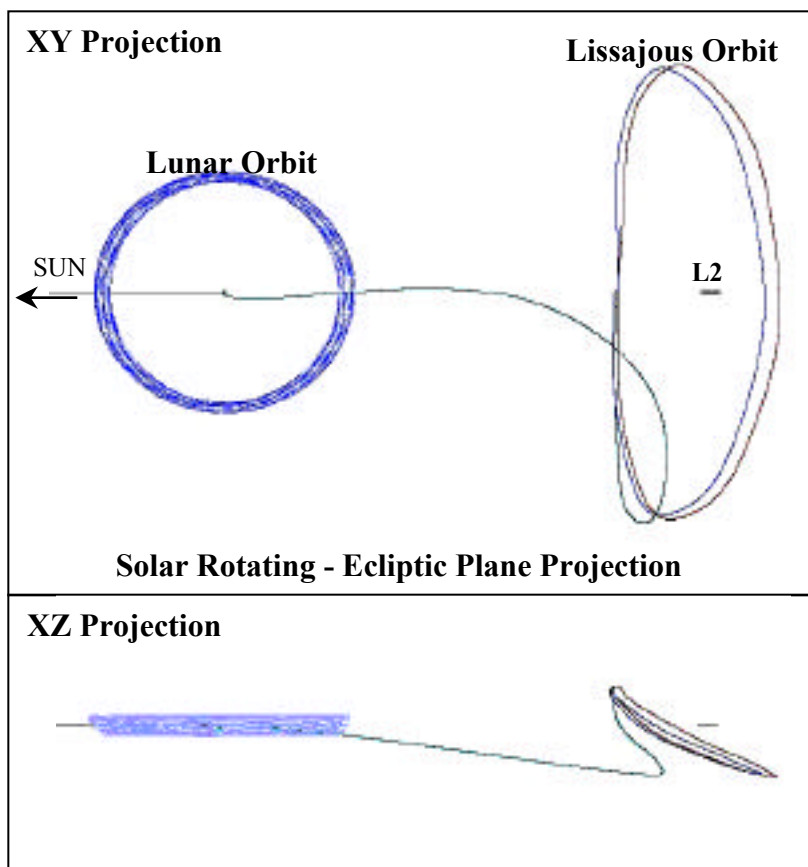
6 Year Evolution



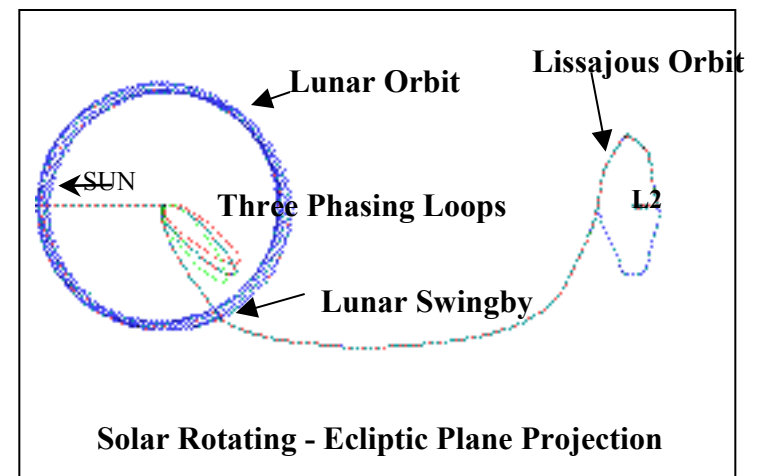
Getting to L2



Direct Injection



Lunar Swingby



XZ Projection



YZ Projection

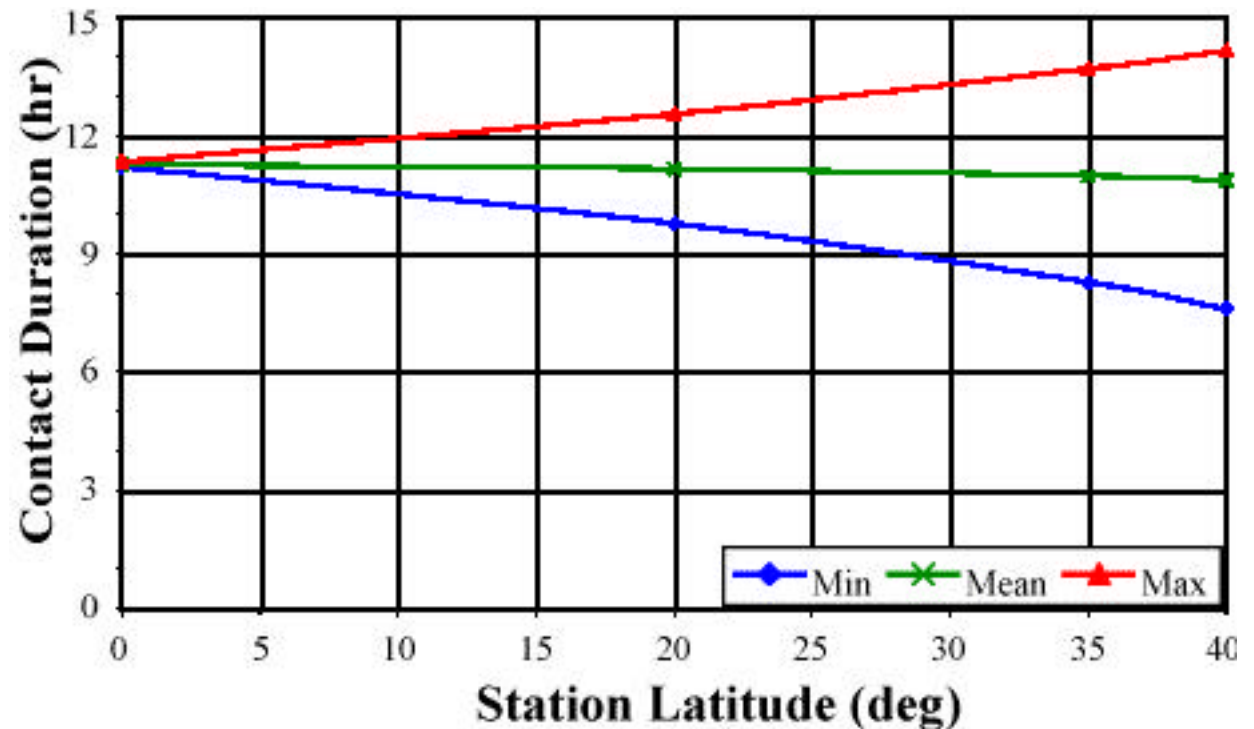




Contacting NGST



- Fortunately, ground contact time to NGST is abundant out at L2
- Coverage ranges from 8 to 14 hours a day depending on the station latitude (assuming a 5° minimum elevation at the station)
- Ranges to NGST are
 - ↳ Minimum: 1.22×10^6 km
 - ↳ Average: 1.53×10^6 km
 - ↳ Maximum: 1.73×10^6 km
- For reference, DSN latitudes at Goldstone, Canberra, and Madrid are 35°, -35°, & 40°, respectively

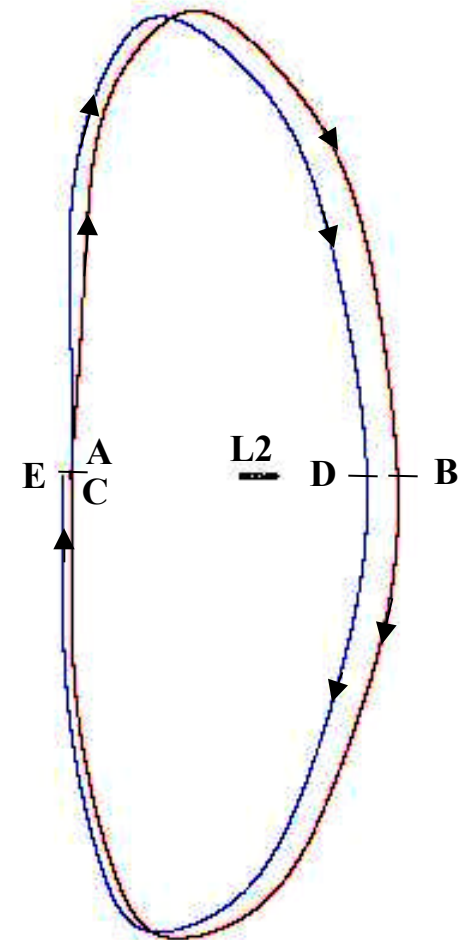




Stationkeeping at L2



- Because of the instabilities of the Lagrangian points, stationkeeping is required to maintain an orbit about L2 for an extended period of time
- At it's simplest, a stationkeeping maneuver is performed at an XZ-plane crossing to provide for a complete revolution about L2 (motion at right is from A → B → C → D → E)
- For example:
 - ↳ a maneuver is performed at point A to ensure a one period revolution to point C
 - ↳ then a maneuver is performed at point B to ensure a one period revolution to point D
 - ↳ etc.
- Typical stationkeeping costs are anywhere from 2 - 4 m/s per year (depending on the requirements)





NGST Wrinkles to Stationkeeping



- The large sun-shade on NGST ($\sim 200 \text{ m}^2$?) provides a continuous perturbation acceleration in the +X direction (away from the Sun) due to solar radiation pressure
- Furthermore, it's now being studied how frequently maneuvers will be needed for momentum unloading
 - ↳ these maneuvers will always be in the +X direction (no thrusters allowed on anti-Sun side of shade)
- As a result inventive methods may be needed to assist with stationkeeping and momentum management
 - ↳ alternate NGST viewing to minimize momentum buildup
 - ↳ use solar shade as 'sail' to supplement stationkeeping options
 - ↳ design gimbaled solar shade to enable solar 'sailing'



References



- ★ Farquhar, R. W., “The Control and Use of Libration-Point Satellites”, NASA Technical Report, NASA TR R-346, September 1970
- ★ Roy, A. E., Orbital Motion, Adam Hilger Ltd., Bristol, 1982
- ★ Szebehely, V., Theory of Orbits: The Restricted Problem of Three Bodies, Academic Press, New York, 1967